Modeling Label Dependencies for Audio Tagging with Graph Convolutional Network

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Abstract—As a multi-label classification task, audio tagging aims to predict the presence or absence of certain sound events in an audio recording. Existing works in audio tagging do not explicitly consider the probabilities of the co-occurrences between sound events, which is termed as the label dependencies in this study. To address this issue, we propose to model the label dependencies via a graph-based method, where each node of the graph represents a label. An adjacency matrix is constructed by mining the statistical relations between labels to represent the graph structure information, and a graph convolutional network (GCN) is employed to learn node representations by propagating information between neighboring nodes based on the adjacency matrix, which implicitly models the label dependencies. The generated node representations are then applied to the acoustic representations for classification. Experiments on Audioset show that our method achieves a state-of-the-art mean average precision (mAP) of 0.434.

Index Terms—Audio tagging, label dependencies, graph convolutional network, representation learning

I. Introduction

AUDIO tagging [1] is the task of predicting the presence or absence of sound events within an audio clip, which has many applications such as information retrieval [2] and music tagging [3]. Compared to single-label audio classification [4], [5], one of the challenges in audio tagging is to deal with the multiple labels in an audio recording.

Recently, convolutional neural networks (CNNs) [6]–[11] and convolutional recurrent neural networks (CRNNs) [12]–[14] provide the state-of-the-art results in audio tagging tasks, which show powerful ability to learn acoustic representations from manually-design features, such as log mel spectrograms. In most previous methods, each sound event type is considered independently, so that audio tagging is treated as a binary classification problem for each sound event type. As a result, the intrinsic relationships between sound events are ignored in these methods. As sound events often co-occur in an audio clip, (*e.g.* when the sound event *piano* appears, *guitar* is more likely to appear than *babycry*), it would be beneficial to take into account the dependencies among labels. Meanwhile, labels often conform to the ontology structure of the abstract sound categories [15]. For example, *snake* can be categorized either as a general category of *animal* or a more specific category of *wild animal*. Some approaches have been proposed to capture the relationships among labels for audio classification. In [16], graph Laplacian regularization was introduced to model the co-occurrence of sound events, and Xu *et al.* [17] proposed a deep neural network (DNN)-based hierarchical learning method for acoustic scene classification. In addition, SONYC Urban Sound Tagging (SONYC-UST) [18] containing 8 coarse-grained classes and 23 fine-grained classes was presented for the DCASE 2019 Urban Sound Tagging Challenge [19]. For large-scale multi-label datasets (*e.g.* Audioset [21]), which contain numerous categories, the hierarchical structures are not clearly pre-defined. However, the implicit label dependencies could be explored to achieve better classification performance.

In this paper, we model the label dependencies via a graph, which has been proven to be effective in capturing the relationships among labels [22]–[24]. The main contribution of this paper is that the implicit dependencies between labels are modeled via GCN with the statistical relations between labels. This is different from two contemporary works [15], [20] brought to our attention where the ontology based domain knowledge is used for the graph construction, rather than the statistical relations exploited in our work. More specifically, each edge in the graph represents the relationships between two nodes, and the adjacency matrix is constructed by the conditional probabilities between labels within the dataset to represent the graph structure information. GCN is employed to learn node representations using the graph structure information, which are then applied to the acoustic representations as the label-wise weights for classification. A single layer GCN learns the representations of each node by aggregating the information of its immediate neighbors. While in multi-layer GCN, information is propagated from more neighbors, hence implicitly modeling the label dependencies. In addition, re-weighting schemes are proposed to alleviate the over-fitting and over-smoothing problems for the adjacency matrix.

II. Graph Convolutional Network

Graph convolutional network (GCN) was presented for semi-supervised learning on graph-structured data [25]. The main idea of GCN is to learn the node representations by aggregating the information of neighboring nodes on a graph $\mathcal{G} = (\mathcal{V}, \mathcal{E})$, with n nodes $v_i \in \mathcal{V}$, edges $(v_i, v_j) \in \mathcal{E}$. Let $\boldsymbol{A} \in \mathbb{R}^{n \times n}$ be the adjacency matrix of $\mathcal{G}$, each GCN layer takes the node representations $\boldsymbol{H}^{(l)} \in \mathbb{R}^{n \times c}$ from the

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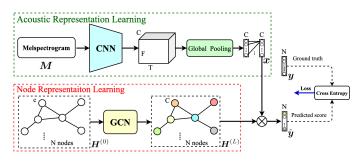
Fig. 1. Overall architecture of our AT-GCN model. Node representations are initially obtained by the word embeddings of the labels and the final node representations learned by GCN are applied to the acoustic representations for classification.
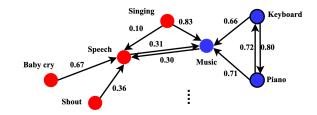

Fig. 2. An example of the graph to model the label dependencies. Each node represents a label and each edge represents the relationships between two nodes, which is determined by the conditional probabilities. Note that the edges with small values of the probabilities are filtered by a re-weighting scheme and not shown in the figure.

previous layer as inputs and outputs updated node representations $\boldsymbol{H}^{(l+1)} \in \mathbb{R}^{n \times c'}$, where c and c' indicate the dimensions of node features in the l-th layer and the $(l+1)$-th layer, respectively. A multi-layer GCN follows the layer-wise propagation rule between the nodes [25]:

$$\boldsymbol{H}^{(l+1)} = h\left(\tilde{\boldsymbol{D}}^{-\frac{1}{2}}\tilde{\boldsymbol{A}}\tilde{\boldsymbol{D}}^{-\frac{1}{2}}\boldsymbol{H}^{(l)}\boldsymbol{W}^{(l)}\right) \quad (1)$$

Here, $\tilde{\boldsymbol{D}}^{-\frac{1}{2}}\tilde{\boldsymbol{A}}\tilde{\boldsymbol{D}}^{-\frac{1}{2}}$ is the normalized symmetric adjacency matrix. $\tilde{\boldsymbol{A}} = \boldsymbol{A} + \boldsymbol{I}_N$ is the adjacency matrix with added self-connections ($\boldsymbol{I}_N$ is the identity matrix) and $\tilde{\boldsymbol{D}}$ is the diagonal degree matrix, where $\tilde{D}_{ii} = \sum_j \tilde{A}_{ij}$. $\boldsymbol{W}^{(l)} \in \mathbb{R}^{c \times c'}$ is a trainable weight matrix, and $h(\cdot)$ denotes an activation function.

III. PROPOSED METHOD

In this section, we present a graph-based method to model the label dependencies for audio tagging. The graph structure is constructed by the statistical relations between the labels, and GCN is employed to learn node representations on the graph. The generated node representations are then applied to the acoustic representations for classification, as detailed next.

A. GCN for Audio Tagging

The overall architecture of our proposed model (AT-GCN) is shown in Fig. 1, and CNN10 [11] is used as the baseline model in our experiments. See [11] for details about CNN10. **Acoustic representation learning** The aim of acoustic representation learning module is to extract the acoustic feature from the input log mel spectrogram, and our proposed AT-GCN has the same acoustic representation learning module as CNN10 [11]. Specifically, convolutional layers are applied to the spectrogram $\boldsymbol{M} \in \mathbb{R}^{t \times f}$, followed by a global pooling layer and a fully-connected layer. Following [11], both maximum and average operations are used for global pooling. Let f_{cnn}, f_{gp}, f_{fc} be the operations of the convolutional layers, the global pooling layer and the fully-connected layer, respectively. The acoustic feature $\boldsymbol{x} \in \mathbb{R}^C$ (where C denotes the dimensionality of the acoustic feature) can be obtained by

$$\boldsymbol{x} = f_{\text{fc}}\left(f_{\text{gp}}\left(f_{\text{cnn}}\left(\boldsymbol{M}; \theta_{\text{cnn}}\right)\right); \theta_{\text{fc}}\right) \quad (2)$$

Here, θ_{cnn} and θ_{fc} denote the model parameters of the convolutional layers and the fully-connected layer, respectively.

Node representation learning GCN is employed to learn node representations in our method. As in (1), the stacked multiple GCN layers are applied where each GCN layer takes the node representations $\boldsymbol{H}^{(l)}$ from the previous layer as inputs and outputs new node representations $\boldsymbol{H}^{(l+1)}$. The input node representations $\boldsymbol{H}^{(0)} \in \mathbb{R}^{N \times c}$ of the first GCN layer are the word embeddings of the labels, where N denotes the number of labels and c is the dimensionality of the embeddings. For the last layer (assuming that the number of layers is L), the output is $\boldsymbol{H}^{(L)} \in \mathbb{R}^{N \times C}$, where C equals the dimensionality of the acoustic feature. The predicted score $\hat{\boldsymbol{y}} \in \mathbb{R}^N$ is then obtained by applying the last node representations to the acoustic representations [28].

$$\hat{\boldsymbol{y}} = \sigma\left(\boldsymbol{H}^{(L)}\boldsymbol{x}\right) \quad (3)$$

where $\sigma(\cdot)$ is the sigmoid function to restrict $\hat{y}^{(i)} \in (0, 1)$. For the given ground truth of the labels within an audio clip $\boldsymbol{y} \in \mathbb{R}^N$ (where $y^{(i)} = \{0, 1\}$ denotes whether label i appears or not), the loss $\mathcal{L}$ is calculated using binary cross-entropy:

$$\mathcal{L} = \sum_{i=1}^{N} y^{(i)} \log\left(\hat{y}^{(i)}\right) + \left(1 - y^{(i)}\right) \log\left(1 - \hat{y}^{(i)}\right) \quad (4)$$

B. Construction of the Graph Structure

The graph structure determines the information propagation between nodes, however, there is no pre-defined graph structure in any audio tagging datasets. In our work, an adjacency matrix is constructed via mining the conditional probabilities between labels within the dataset to represent the graph structure information, as shown in Fig. 2.

Firstly, we count the occurrence of label pairs in the training set and get the matrix $\boldsymbol{X} \in \mathbb{R}^{N \times N}$ (where N indicates the number of labels, and X_{ij} denotes the co-occurring times of label L_i and L_j). Then, the occurrence times of the labels in the training set are counted and the conditional probability matrix can be calculated by

$$P_{ij} = X_{ij}/T_i \quad (5)$$

where T_i denotes the occurrence times of label L_i in the training set, $P_{ij} = P\left(L_j | L_i\right)$ means the probability of label L_j when label L_i appears. Note that P_{ij} is not equal to P_{ji} since T_i is not the same as T_j.

However, the conditional probabilities between labels in the training and test set may not be completely consistent, and some small probabilities may become noise. Thus, it is necessary to alleviate over-fitting of the adjacency matrix. Specifically, a threshold τ is applied to filter noisy edges:

$$A_{ij} = \begin{cases} 0, & \text{if } P_{ij} < \tau \\ P_{ij}, & \text{if } P_{ij} \geq \tau \end{cases} \tag{6}$$

where A is the re-weighted adjacency matrix.

Another potential problem is over-smoothing, *i.e.* as the GCN layer deepens, the node features may be over-smoothed and nodes from different clusters may become indistinguishable [26], [27]. Thus, we adjust the information propagation among nodes in GCN by another re-weighting scheme:

$$A'_{ij} = \begin{cases} pA_{ij}/\sum_{\substack{j=1 \\ i \neq j}}^{N} A_{ij}, & \text{if } i \neq j \\ 1 - p, & \text{if } i = j \end{cases} \tag{7}$$

where A' is the re-weighted and normalized adjacency matrix, and p determines the weights assigned to a node itself and its neighbors. When $p \to 0$, the neighboring information tends to be ignored. On the contrary, when $p \to 1$, the information of a node itself will not be considered.

The proposed algorithm is summarized in Algorithm 1.

Algorithm 1 AT-GCN

Input: The log mel spectrogram M; The initial node representations $H^{(0)}$;
Output: The predicted score $\hat{y}$;
1: Calculate the adjacency matrix A using equation (5)-(7);
2: Extract the acoustic representation x using equation (2);
3: **for** $l = 0, \ldots, L - 1$ **do**
4:     Get the node representations of the next layer $H^{(l+1)}$ using equation (1);
5: **end for**
6: Calculate $\hat{y}$ according to equation (3);
7: **return** $\hat{y}$;

IV. EXPERIMENTS

A large-scale multi-label dataset (Audioset [21]) is used in our experiments to evaluate our method, which is one of the most challenging datasets for audio tagging [1]. Log mel spectrograms are extracted from the audio signals as the input of the networks. The details are as follows.

A. Dataset, Metrics and Preprocessing

Dataset Audioset [21] is a large-scale dataset with over 2 million 10-second audio clips from YouTube videos, with a total of 527 categories. The training set consists of 2,063,839 audio clips including a balanced subset of 22,160 audio clips. The evaluation set consists of 20,371 audio clips. Following [14], both the balanced and unbalanced training sets are used for training, with one part taken as our validation set. The evaluation set is used as the test set in our experiments.
Metrics Mean average precision (mAP), mean area under the curve (mAUC) and d-prime are used as our evaluation metrics.

TABLE I
COMPARISON OF PERFORMANCE ON AUDIOSET

Model	Depth	mAP	mAUC	d-prime
Google CNN (2017) [21]	-	0.314	0.959	2.452
Multi-level attention (2018) [9]	-	0.360	0.970	2.660
Multi-level attention* (2018) [9]	-	0.362	0.970	2.667
TAL Net (2019) [14]	-	0.362	0.965	2.554
TAL Net* (2019) [14]	-	0.367	0.969	2.638
DeepRes (2019) [5]	-	0.392	0.971	2.682
CNN10* (2019) [11]	-	0.422	0.970	2.653
AT-GCN (ours)	1-layer	0.428	0.971	2.711
	2-layers	**0.434**	**0.974**	**2.736**
	3-layers	0.430	0.972	2.715

*The listed results of Multi-level attention [9], TAL Net [14] and CNN10 [11] are obtained under the same experimental setups as AT-GCN (e.g. using preprocessing and data augmentation). The original Multi-level attention [9] and TAL Net [14] did not use data augmentation.

TABLE II
ACCURACY COMPARISONS ON DIFFERENT CONSTRUCTION METHODS OF THE ADJACENCY MATRIX

Construction Method	mAP	mAUC	d-prime
AT-GCN w/ method in [15], [28]	0.431	0.973	2.727
AT-GCN w/ method in [20]	0.429	0.971	2.701
AT-GCN w/o scheme	0.132	0.907	1.872
AT-GCN w/ scheme in (6)	0.267	0.952	2.360
AT-GCN w/ scheme in (7)	0.188	0.932	2.113
AT-GCN w/ scheme in (6) & (7)	**0.434**	**0.974**	**2.736**

These metrics are calculated on individual classes and then averaged across all classes.
Preprocessing Limited by the computation resource, the pre-extracted log mel spectrograms [14] with window size 50ms and hop length 25ms are used in our experiments instead of the raw audio signals, which have lower time domain resolution than those used in [11]. The number of Mel bands is set to 64 and the size of a log mel spectrogram is 400×64.

B. Implementation Details

AT-GCN The node representation learning module of our AT-GCN [1] consists of two GCN layers with output dimensionality of 256 and 512. It was proven that the performance is hardly impacted by the different initial label representations [28], and following [28], the word embeddings of 300-dim GloVe[2] [29] are used as the initial label representations in our experiments. The dimensionality of the acoustic representation is set to 512 for a fair comparison with CNN10 [11], and the hyperparameters τ in (6) and p in (7) are set to 0.3 and 0.2 empirically based on the validation set. PReLU [30] with the negative slope of 0.2 is used as the activation function in (1).
Training details In the training phase, the Adam [31] is employed as the optimizer with a learning rate of 0.001. Batch size is set to 64 and training takes 600,000 iterations. Following [11], data augmentation methods mixup [32] and SpecAugment [33] are applied in our experiments to prevent the system from over-fitting and improve the performance.

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[1]https://github.com/WangHelin1997/AT-GCN
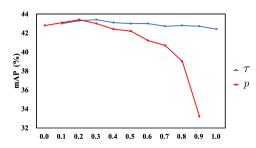[2]https://github.com/stanfordnlp/GloVe

Fig. 3. Accuracy comparisons of different values of τ and p for AT-GCN with two GCN layers (metric: mAP). Note that when $\tau = 1.0$, $\tilde{\boldsymbol{D}}^{-\frac{1}{2}} \tilde{\boldsymbol{A}} \tilde{\boldsymbol{D}}^{-\frac{1}{2}}$ in (1) becomes the identity matrix. AT-GCN degenerates to a structure almost identical to CNN10, but with an extra fully-connected layer (as a GCN layer degenerates to a fully-connected layer). As a consequence, the mAP result (42.3%) by AT-GCN is slightly different from that of CNN10 (42.2%).
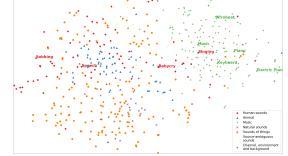
C. Experimental Results and Analysis

Table I demonstrates the performance of our proposed AT-GCN and other state-of-the-art methods on the Audioset. The results indicate that the proposed AT-GCN outperforms all the compared methods, which confirms the effectiveness of modeling the label dependencies. A single layer GCN learns the node representations by aggregating the information of the immediate neighbors guided by the graph structure information. The results show that AT-GCN with one GCN layer achieves a better performance than the baseline model (CNN10) owing to these statistical relations, which is similar to [16]. While in multi-layer GCN, information is propagated from more neighbors, which implicitly models the deep label dependencies and offers more performance gain. However, increasing the number of GCN layers may lead to over-smoothing [34], which may mix the features of too many nodes and make them indistinguishable. It can be observed that AT-GCN with two GCN layers provides a good trade-off in these aspects and achieves the best performance.

In order to analyze the impacts of the formulation of the adjacency matrix, ablation experiments are carried out. As shown in Table II, AT-GCN does not perform well when no re-weighting scheme is applied because of the over-fitting and over-smoothing problems, which are discussed in Section III-B. In [15], [28], a threshold is set to filter the noisy edges and other edges are treated equally, which is achieved by binarizing the adjacency matrix. However, our proposed re-weighting schemes retain the information of the other edges by only re-weighting the noisy edges and obtain better performance. Both the re-weighting schemes in (6) and (7) improve the performance, and a higher performance can be achieved with the combination of them. In addition, we have tested another construction method of the adjacency matrix [20], which utilizes the ontology rather than the statistical relations. Our proposed method achieves better performance, which shows that the label dependencies are more important in the large-scale multi-label dataset (i.e. Audioset).
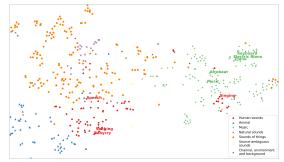
In addition, we vary the values of the hyperparameters τ in (6) and p in (7) to analyze the effects, and show the results in Fig. 3. As the values of τ and p increase, the accuracy is boosted and then drops, which achieves the peek accuracy when $\tau = 0.3$ and $p = 0.2$. τ is the threshold to filter the

(a) t-SNE on the weights of the last fully-connected layer of CNN10

(b) t-SNE on the last node representations learned by AT-GCN

Fig. 4. Visualization of the last node representations learned by AT-GCN and the learned weights of the last fully-connected layer of CNN10 on Audioset. Note that Audioset [21] contains 527 classes (527 dots in the figure) with 7 general categories (the same color dots in the figure). Here, 9 classes are marked as examples.

edges, and the small values of τ mean the edges of small probabilities (i.e. noisy edges) are filtered. However, when too many edges are filtered, the correlated neighbors will be ignored as well which decreases the accuracy. p determines the balance between a node itself and its neighbors when updating the node features. If p is too small, the nodes of the graph cannot get sufficient information from correlated nodes. On the other hand, it will lead to over-smoothing if p is too large.

Furthermore, the t-SNE [36] is adopted to visualize the last node representations (i.e. $\boldsymbol{H}^{(L)}$ in (3)) learned by our proposed AT-GCN as well as the weights of the last fully-connected layer of CNN10, with the results shown in Fig. 4. It can be observed that CNN10 can learn some meaningful relationships among the labels, such as the cluster pattern of the general category *music*. However, the other cluster patterns are not clear and the semantic related labels (e.g. *sobbing* and *babycry*) are not close in the label space. In contrast, AT-GCN shows less divergence in the label space and exhibits more clear cluster patterns. Specifically, the semantic related labels (such as *piano* and *keyboard*, *sobbing* and *babycry*) tend to be much closer in the label space than CNN10, which shows the effectiveness of modeling the label dependencies.

V. CONCLUSION

In this paper, a novel audio-tagging method (AT-GCN) has been proposed where the implicit dependencies between the labels are modeled by a graph convolutional network. Our proposed method achieves the state-of-art performance on the Audioset.

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